

# THE DECOUPLING OF LINEAR SYSTEMS

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The purpose of this presentation is to report on the development of a method and algorithm to decouple any linear system. To be specific, let  $\mathbf{A}$ ,  $\mathbf{B}$  and  $\mathbf{C}$  be arbitrary square matrices of the same order with at least one of the matrices, say  $\mathbf{A}$ , being nonsingular. An invertible transformation is developed to convert  $\mathbf{A}\ddot{\mathbf{q}} + \mathbf{B}\dot{\mathbf{q}} + \mathbf{C}\mathbf{q} = \mathbf{f}(t)$  into  $\ddot{\mathbf{p}} + \mathbf{D}\dot{\mathbf{p}} + \mathbf{\Omega}\mathbf{p} = \mathbf{g}(t)$  for which  $\mathbf{D}$ ,  $\mathbf{\Omega}$  are diagonal. The decoupling procedure is an extension of classical modal analysis, which is a time-honored method for decoupling linear dynamical systems that are either undamped or classically damped.